Reflection or refraction at a plane surface: When rays diverge from an object point $P$ and are reflected or refracted, the directions of the outgoing rays are the same as though they had diverged from a point $P^{\prime}$ called the image point. If they actually converge at $P^{\prime}$ and diverge again beyond it, $P^{\prime}$ is a real image of $P$; if they only appear to have diverged from $P^{\prime}$, it is a virtual image. Images can be either erect or inverted.


Lateral magnification: The lateral magnification $m$ in any reflecting or refracting situation is defined as the ratio of

$$
\begin{equation*}
m=\frac{y^{\prime}}{y} \tag{34.2}
\end{equation*}
$$ image height $y^{\prime}$ to object height $y$. When $m$ is positive, the image is erect; when $m$ is negative, the image is inverted.



Focal point and focal length: The focal point of a mirror is the point where parallel rays converge after reflection from a concave mirror, or the point from which they appear to diverge after reflection from a convex mirror. Rays diverging from the focal point of a concave mirror are parallel after reflection; rays converging toward the focal point of a convex mirror are parallel after reflection. The distance from the focal point to the vertex is called the focal length, denoted as $f$. The focal points of a lens are defined similarly.


Relating object and image distances: The formulas for object distance $s$ and image distance $s^{\prime}$ for plane and spherical mirrors and single refracting surfaces are summarized in the table. The equation for a plane surface can be obtained from the corresponding equation for a spherical surface by setting $R=\infty$. (See Examples 34.1-34.7.)


|  | Plane Mirror | Spherical Mirror | Plane Refracting <br> Surface | Spherical <br> Refracting Surface |
| :--- | :--- | :--- | :--- | :--- |
| Object and image distances | $\frac{1}{s}+\frac{1}{s^{\prime}}=0$ | $\frac{1}{s}+\frac{1}{s^{\prime}}=\frac{2}{R}=\frac{1}{f}$ | $\frac{n_{a}}{s}+\frac{n_{b}}{s^{\prime}}=0$ | $\frac{n_{a}}{s}+\frac{n_{b}}{s^{\prime}}=\frac{n_{b}-n_{a}}{R}$ |
| Lateral magnification | $m=-\frac{s^{\prime}}{s}=1$ | $m=-\frac{s^{\prime}}{s}$ | $m=-\frac{n_{a} s^{\prime}}{n_{b} s}=1$ | $m=-\frac{n_{a} s^{\prime}}{n_{b} s}$ |

Object-image relationships derived in this chapter are valid for only rays close to and nearly parallel to the optic axis; these are called paraxial rays. Nonparaxial rays do not converge precisely to an image point. This effect is called spherical aberration.

Thin lenses: The object-image relationship, given by Eq. (34.16), is the same for a thin lens as for a spherical mirror. Equation (34.19), the lensmaker's equation, relates the focal length of a lens to its index of refraction and the radii of curvature of its surfaces. (See
Examples 34.8-34.11.)

$$
\begin{align*}
& \frac{1}{s}+\frac{1}{s^{\prime}}=\frac{1}{f}  \tag{34.16}\\
& \frac{1}{f}=(n-1)\left(\frac{1}{R_{1}}-\frac{1}{R_{2}}\right) \tag{34.19}
\end{align*}
$$



Sign rules: The following sign rules are used with all plane and spherical reflecting and refracting surfaces:

- $s>0$ when the object is on the incoming side of the surface (a real object); $s<0$ otherwise.
- $s^{\prime}>0$ when the image is on the outgoing side of the surface (a real image); $s^{\prime}<0$ otherwise.
- $R>0$ when the center of curvature is on the outgoing side of the surface; $R<0$ otherwise.
- $m>0$ when the image is erect; $m<0$ when inverted.

